

Heavy-Atom Isotope Effects

k_H/k_D provides large change in reduced mass, but other isotope effects also studied.

isotope effect typical maximum value

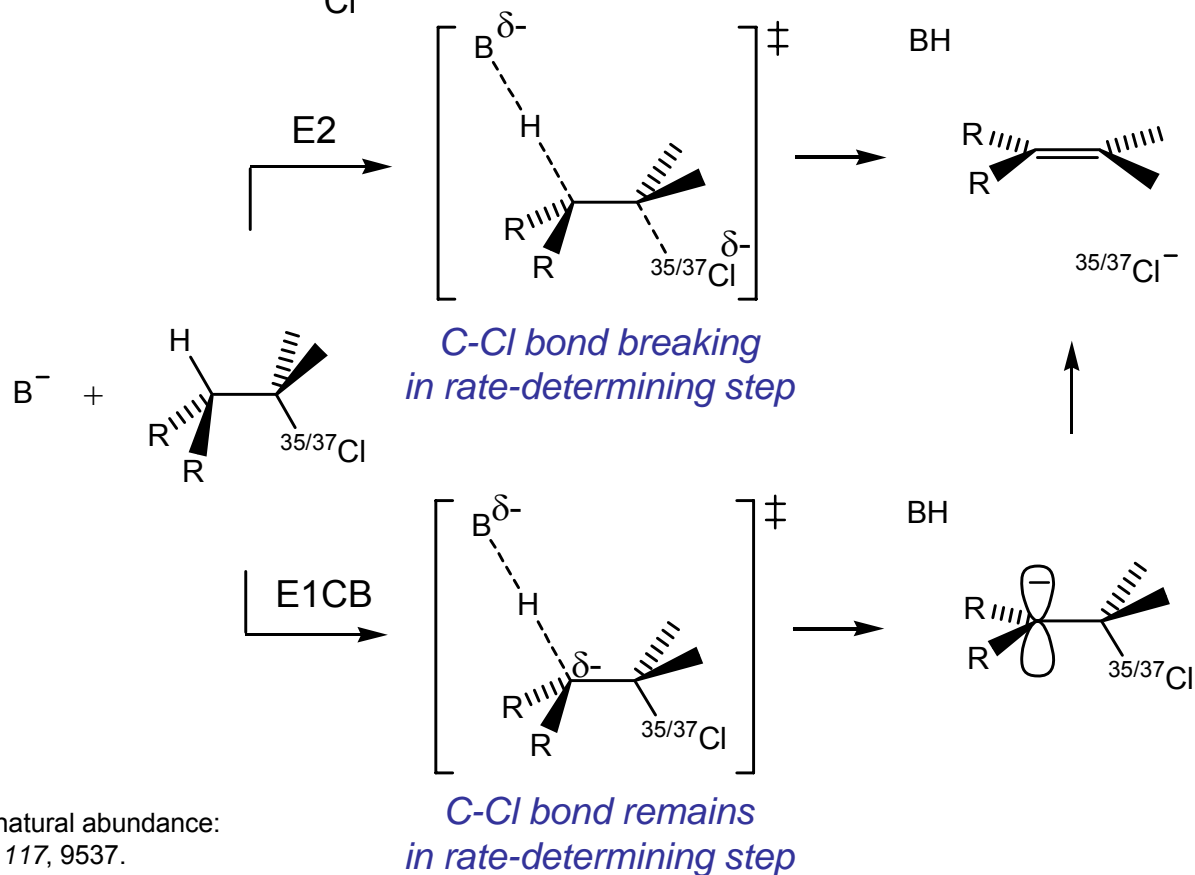
$$\frac{k_{^{12}\text{C}}}{k_{^{13}\text{C}}} \sim 1.04$$

$$\frac{k_{^{12}\text{C}}}{k_{^{14}\text{C}}} \sim 1.07$$

$$\frac{k_{^{14}\text{N}}}{k_{^{15}\text{N}}} \sim 1.03$$

$$\frac{k_{^{16}\text{O}}}{k_{^{18}\text{O}}} \sim 1.03$$

Example: $\frac{k_{^{35}\text{Cl}}}{k_{^{37}\text{Cl}}}$



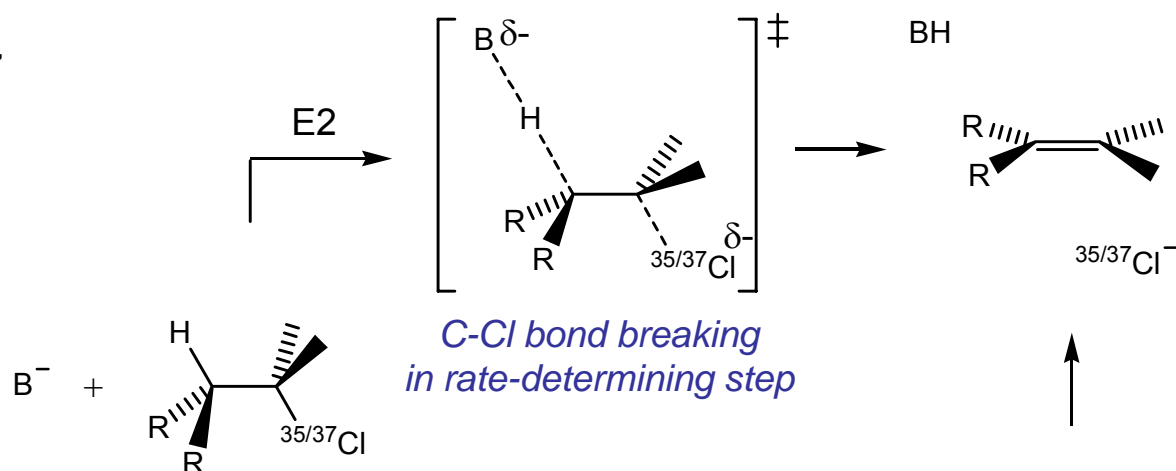
Method for measuring heavy isotope effects at natural abundance:
Singleton, D. A. et al. *J. Am. Chem. Soc.* **1995**, 117, 9537.

Heavy-Atom Isotope Effects

k_H/k_D provides large change in reduced mass, but other isotope effects also studied.

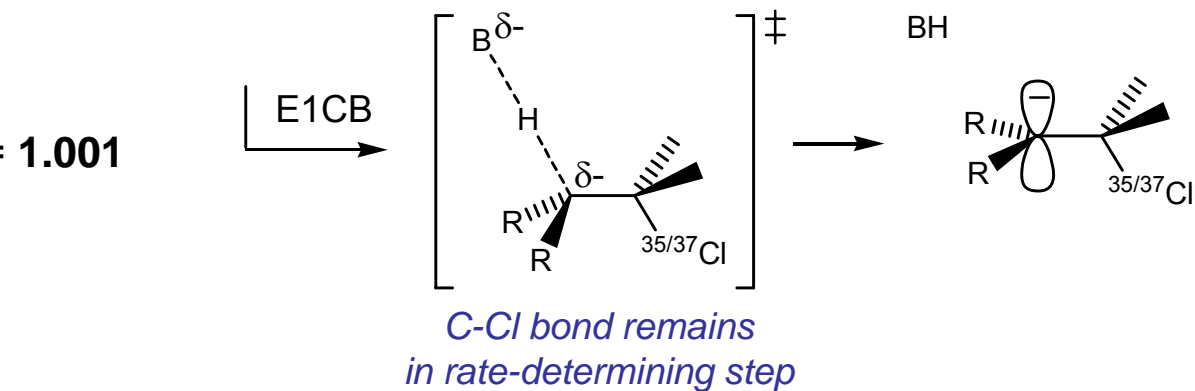
$$R = \text{CH}_3 \quad \frac{k_{^{35}\text{Cl}}}{k_{^{37}\text{Cl}}} = 1.007$$

(follows E2)



$$R = (p\text{-NO}_2)\text{Ph} \quad \frac{k_{^{35}\text{Cl}}}{k_{^{37}\text{Cl}}} = 1.001$$

(follows E1CB;
carbanion stabilized
by Ph groups)



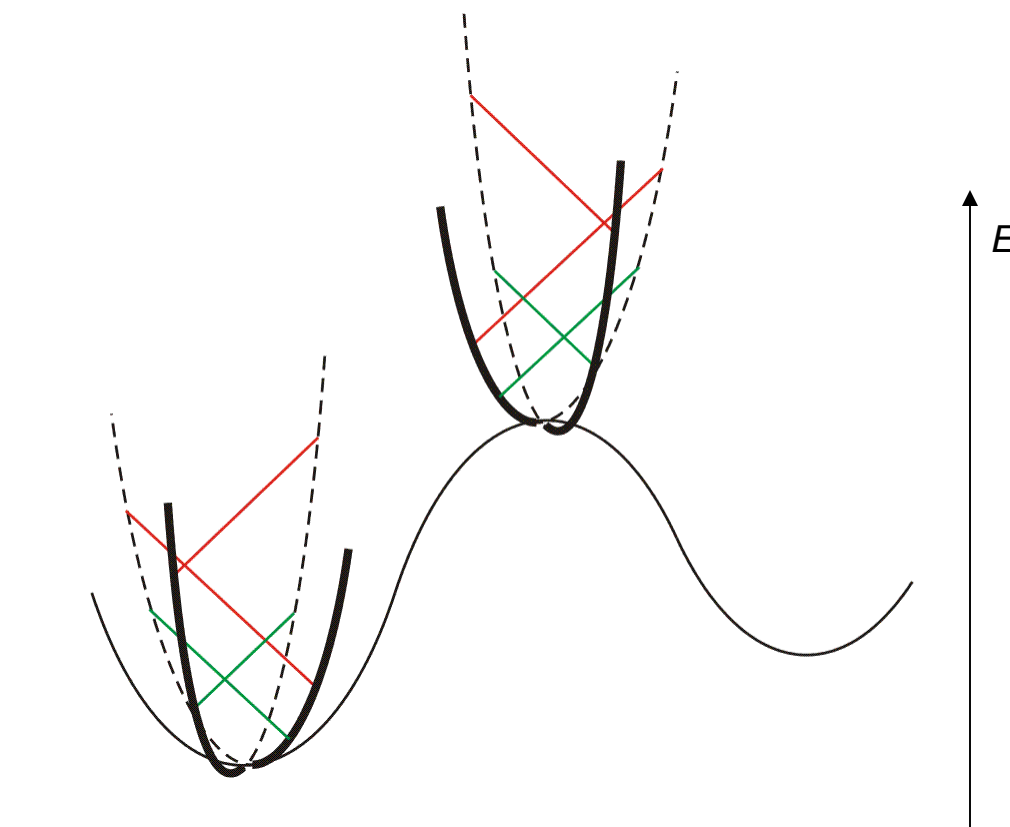
Calculating Isotope Effects

$$\left(\frac{k_H}{k_D}\right)_{\text{overall, for } n \text{ modes}} = \left(\frac{k_H}{k_D}\right)_{v_1} \left(\frac{k_H}{k_D}\right)_{v_2} \cdots \left(\frac{k_H}{k_D}\right)_{v_n}$$

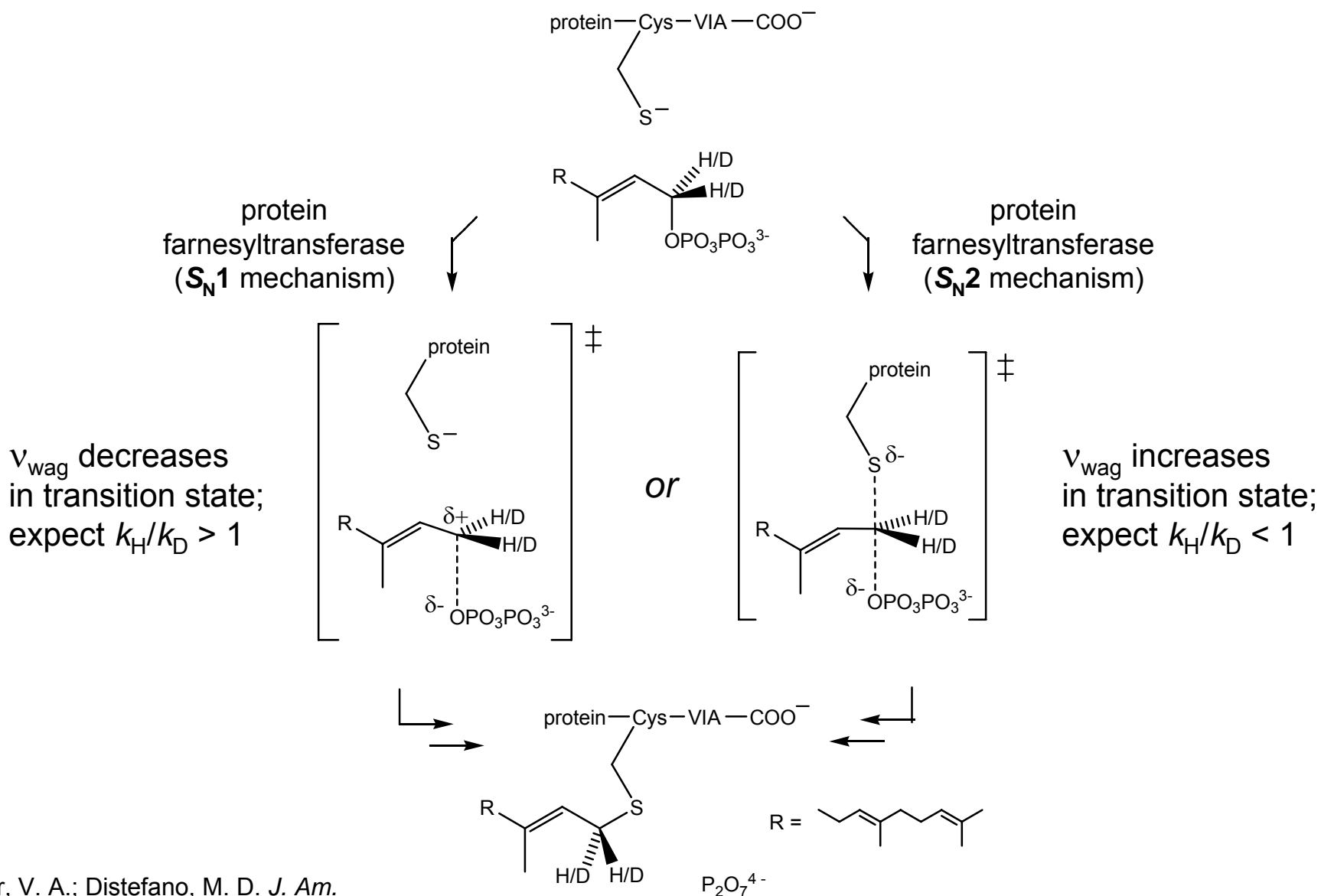
For simplicity, we have tried to identify one major component to isotope effect;

But, there may be multiple components.

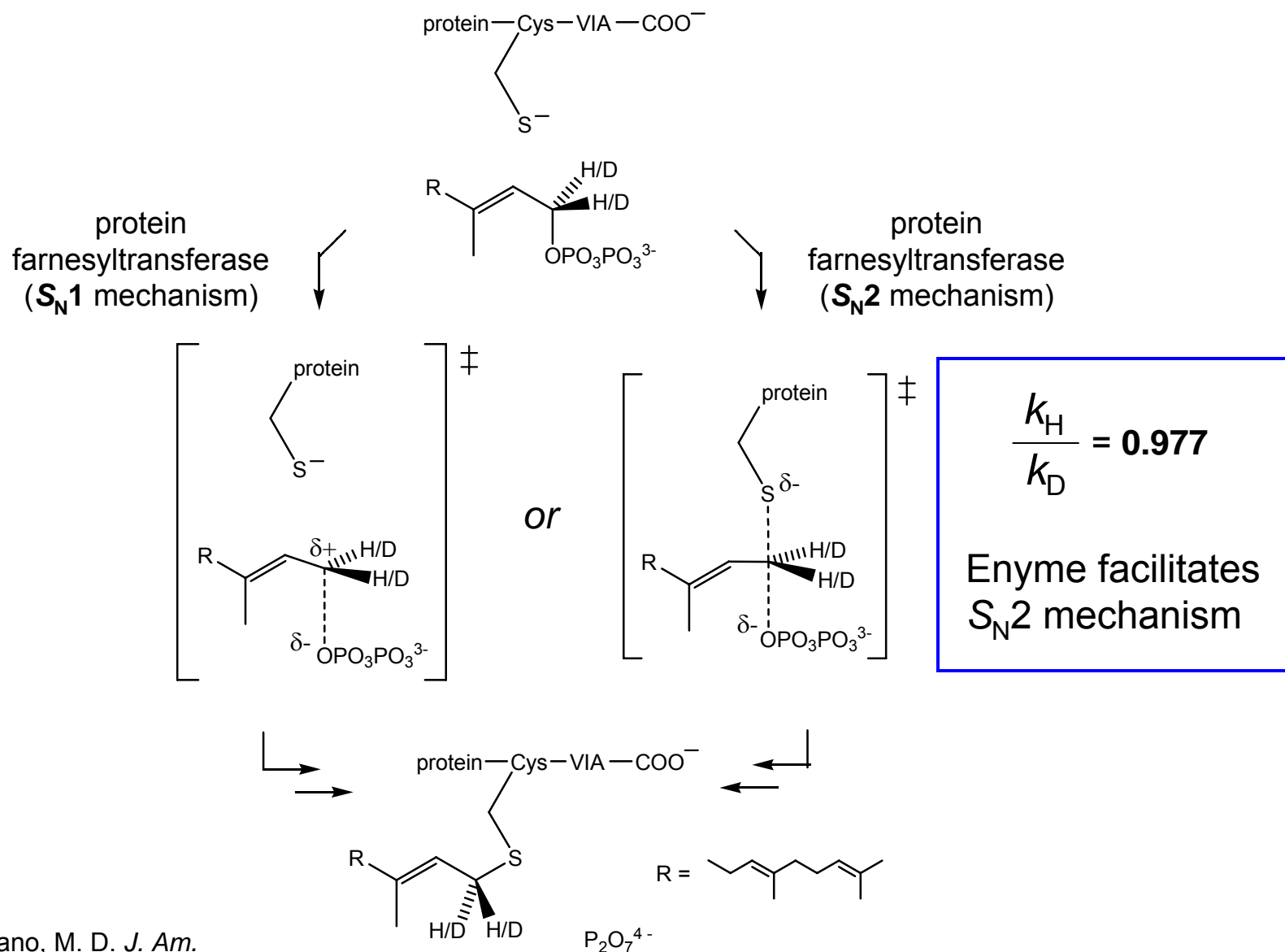
Computational methods for calculating isotope effects for all vibrational modes are available.



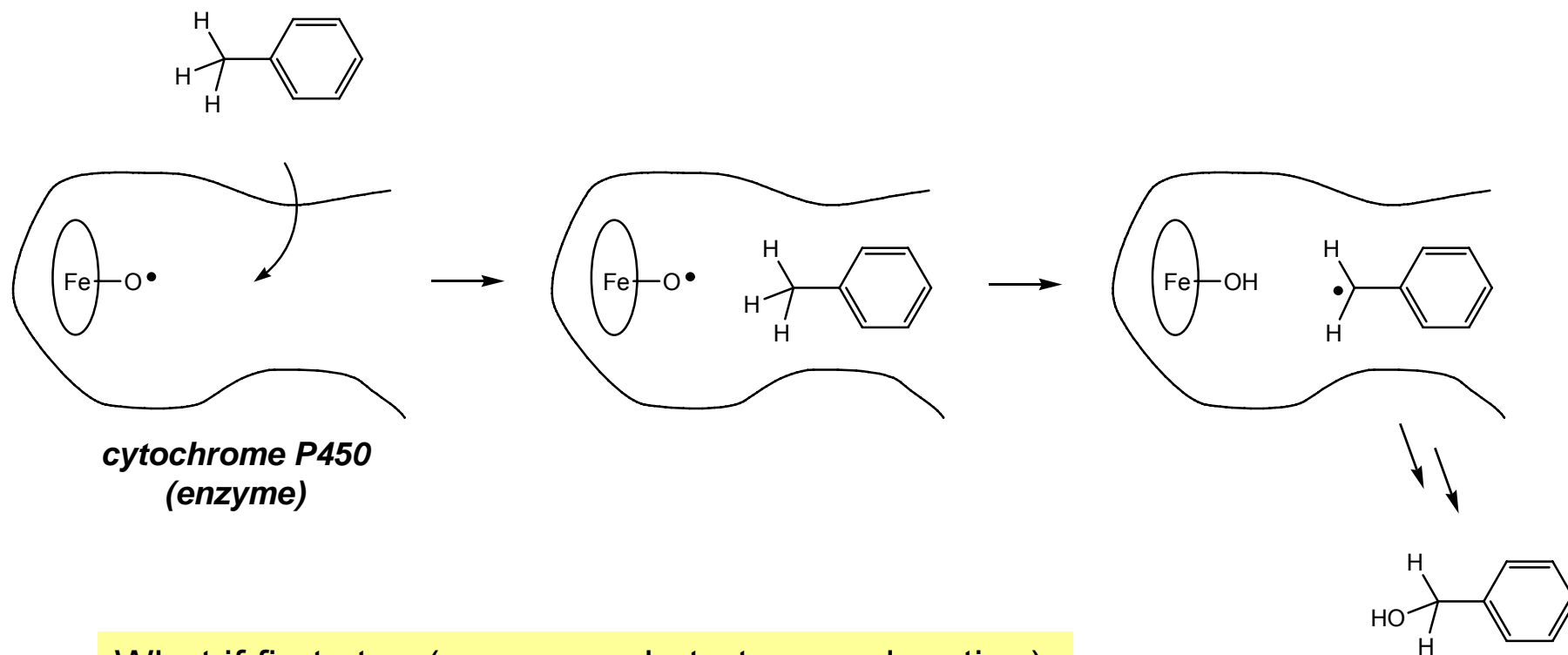
Isotope Effects and Enzyme Mechanisms



Isotope Effects and Enzyme Mechanisms

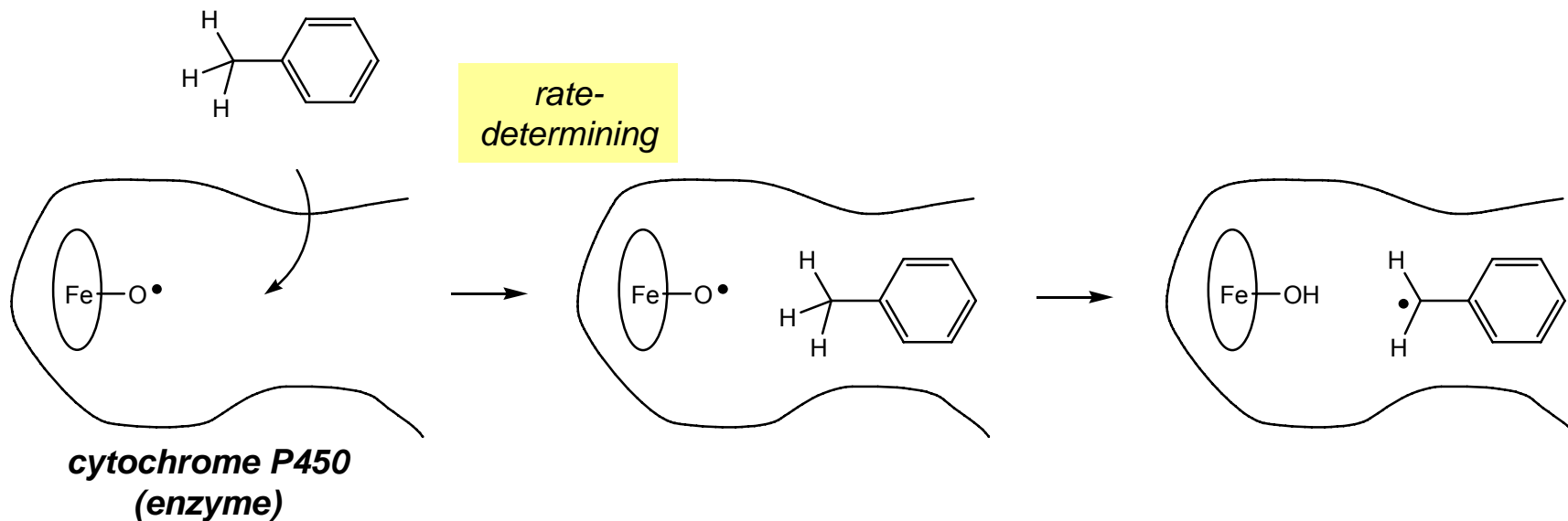


Intra- vs. Inter-molecular Isotope Effects: Probing Non-Rate-Determining Steps



What if first step (enzyme-substrate complexation) is rate-determining?
How do we find out about mechanism of subsequent steps?

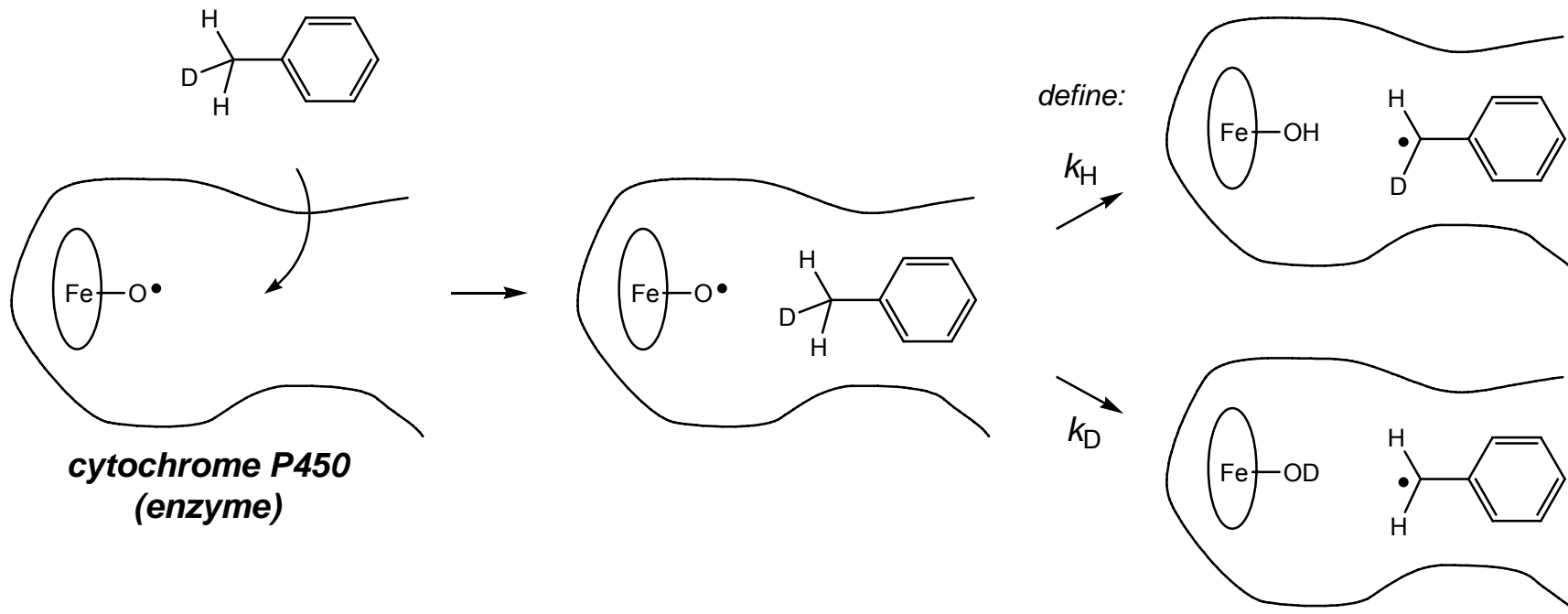
Intra- vs. Inter-molecular Isotope Effects: Probing Non-Rate-Determining Steps



For *intermolecular*
comparison,
would expect

$$\frac{k_H}{k_D} = \frac{-\frac{\partial \left[\text{H-CH}_2\text{-C}_6\text{H}_5 \right]}{\partial t}}{-\frac{\partial \left[\text{D}_3\text{-C-CH}_2\text{-C}_6\text{H}_5 \right]}{\partial t}} = \frac{\frac{\partial \left[\text{HO-CH}_2\text{-C}_6\text{H}_5 \right]}{\partial t}}{\frac{\partial \left[\text{DO-CH}_2\text{-C}_6\text{H}_5 \right]}{\partial t}} \approx 1$$

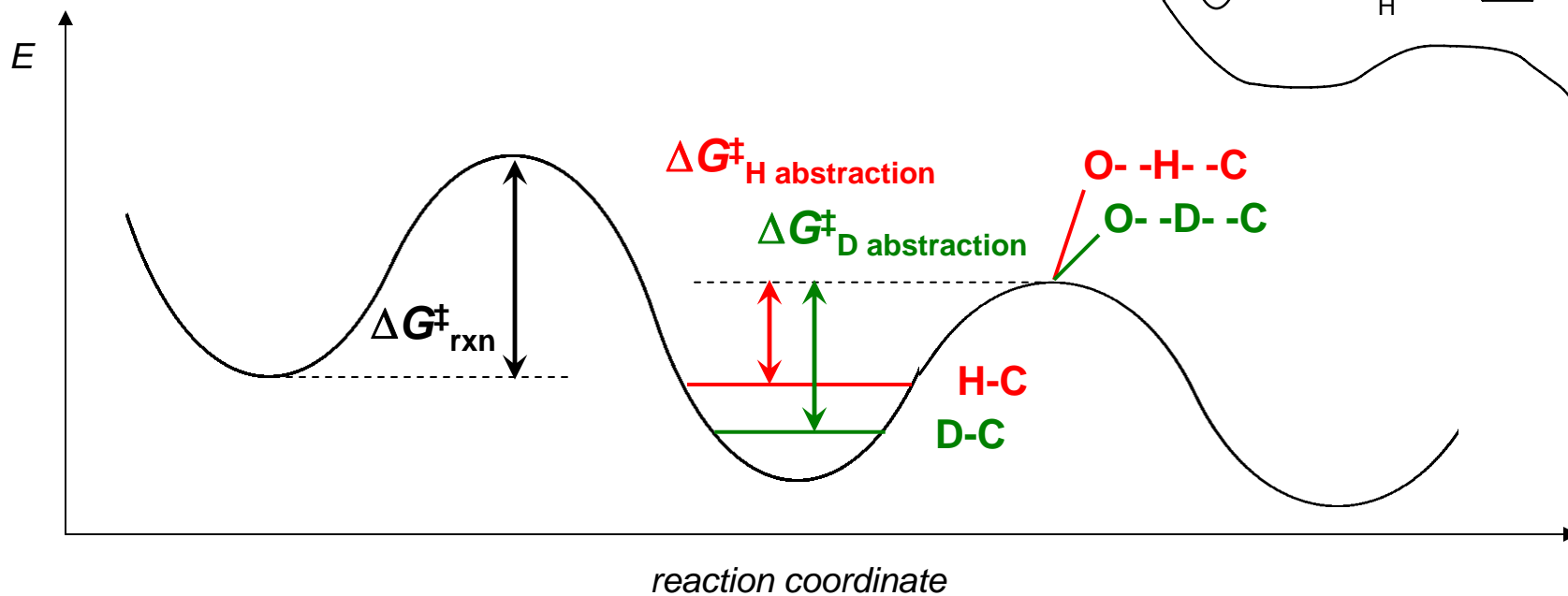
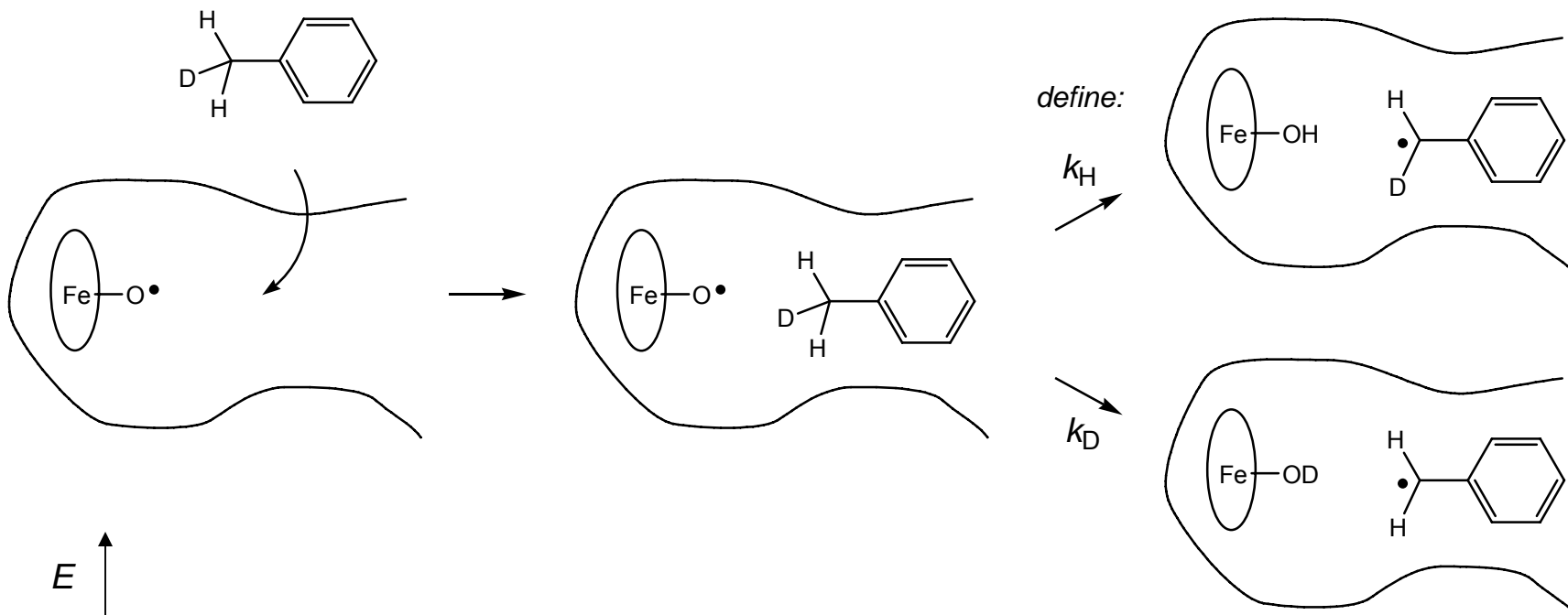
Intra- vs. Inter-molecular Isotope Effects: Probing Non-Rate-Determining Steps



For *intramolecular* comparison, what would we expect for

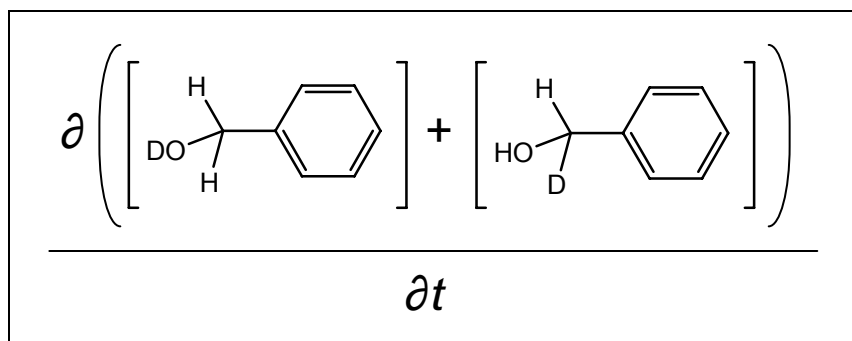
$$\frac{k_H}{k_D} = \frac{\frac{\partial \left[\text{HO}-\text{CH}(\text{D})-\text{C}_6\text{H}_5 \right]}{\partial t}}{\frac{\partial \left[\text{DO}-\text{CH}(\text{H})-\text{C}_6\text{H}_5 \right]}{\partial t}} \quad ??$$

Intramolecular Isotope Effects

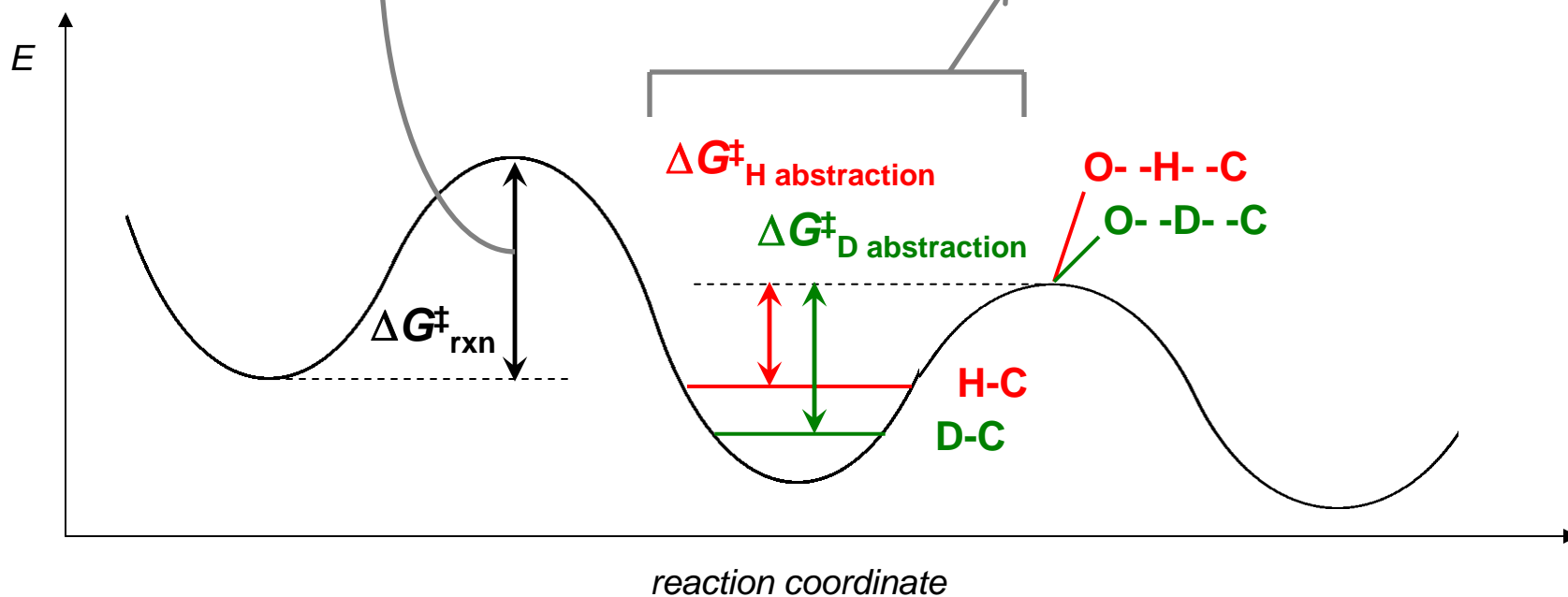
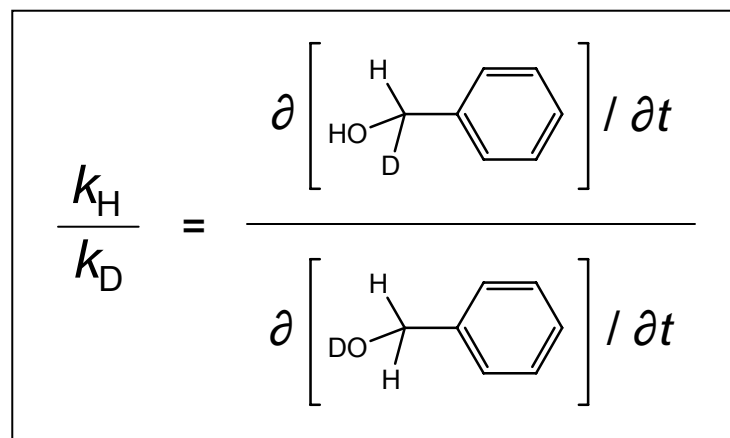


Intramolecular Isotope Effects

determines overall rate

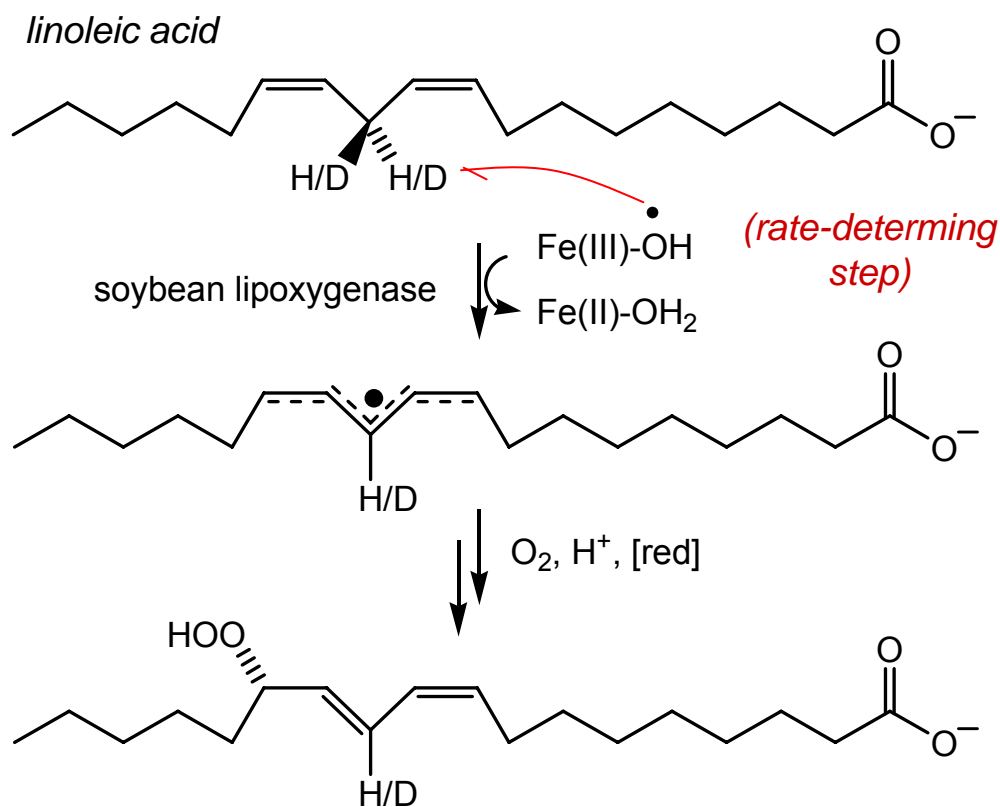


determines product ratio



Isotope Effects and Tunneling

Occasionally, isotope effects are too large to explain with vibrational mode analysis.



$$\frac{k_H}{k_D} = 81 (!)$$

Explanation:

Isotope effect from differing abilities of H & D to “tunnel” through kinetic reaction barrier.

See: Kohen, A.; Klinman, J. P. *Chem. Biol.* **1999**, *6*, R191-R198;
Kohen, A.; Klinman, J. P. *Acc. Chem. Res.* **1998**, *31*, 397-404.

Isotope Effects and Tunneling

de Broglie Wavelength:

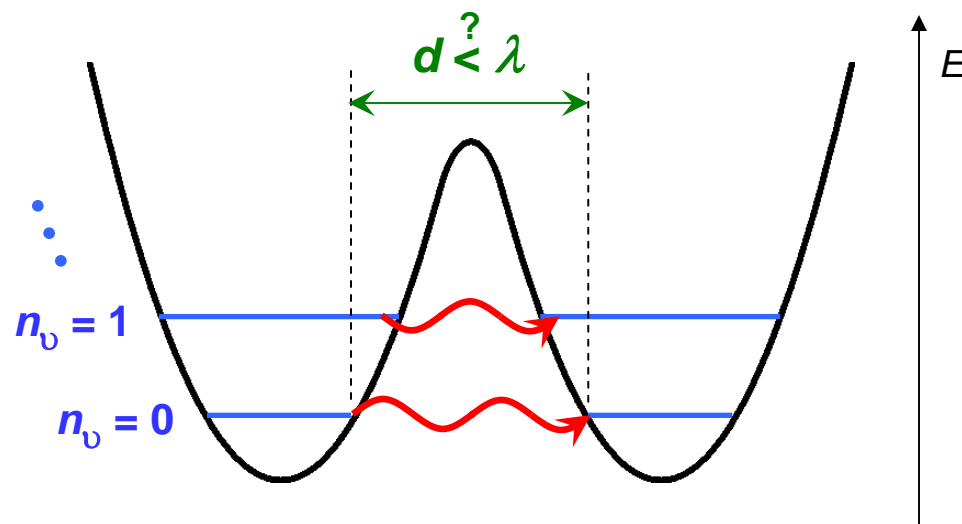
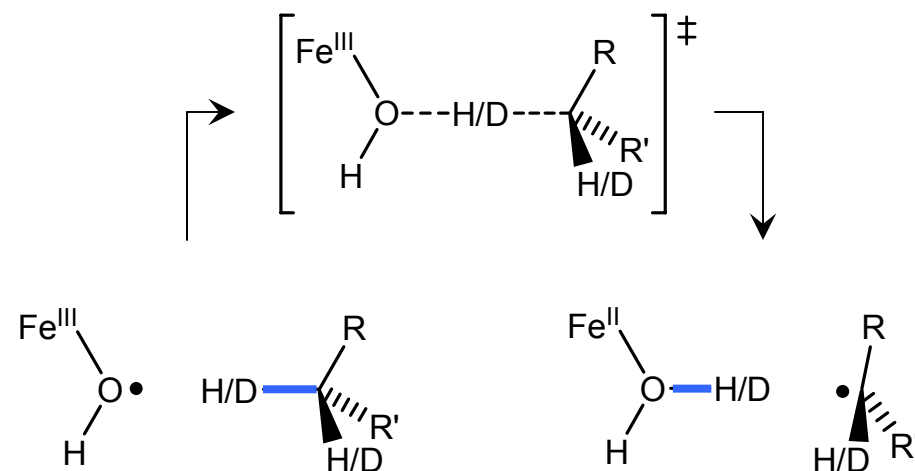
$$\lambda = \frac{h}{mv} = \frac{h}{\sqrt{2mkT}}$$

$$\lambda(\text{H}) = 1.8 \text{ \AA} \text{ (at 298 K)}$$

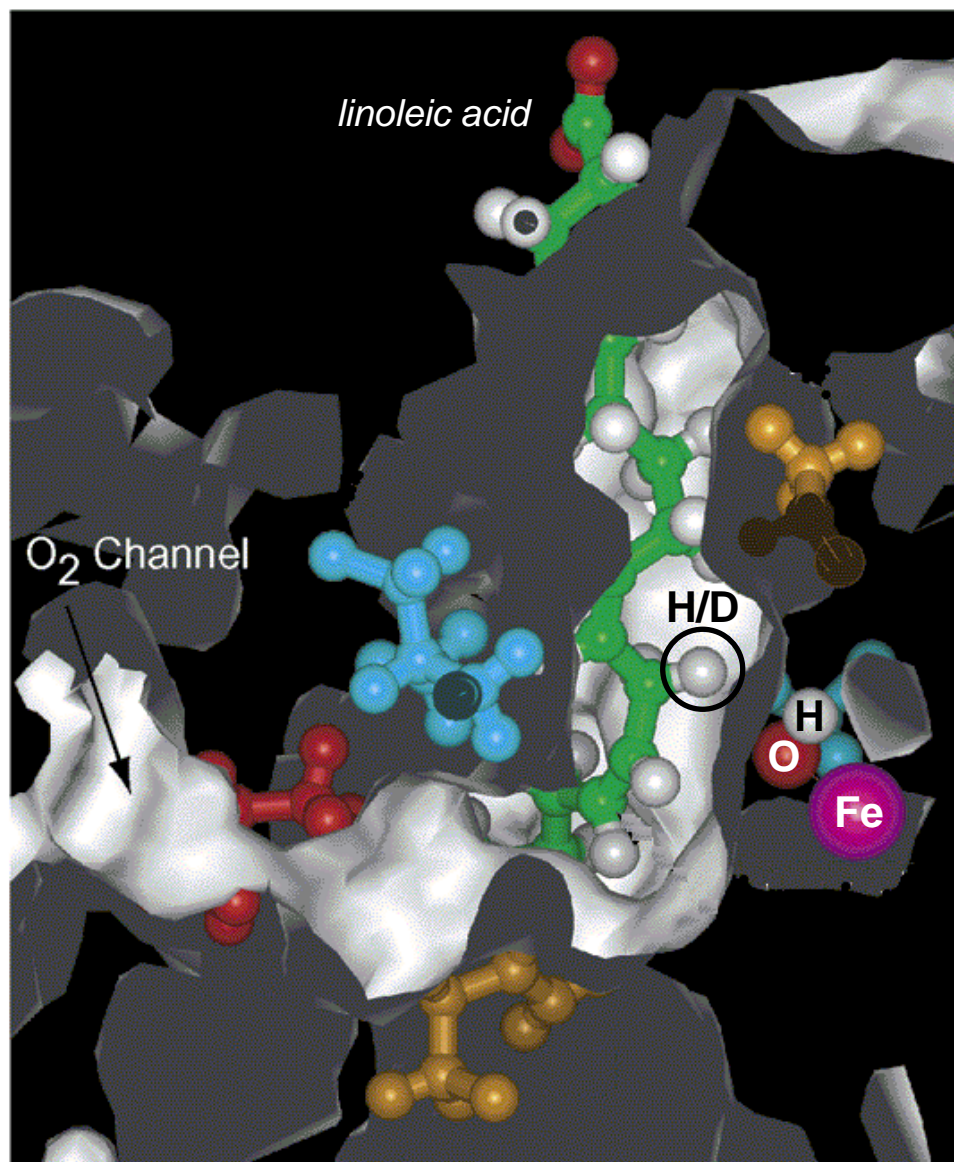
$$\lambda(\text{D}) = 1.2 \text{ \AA}$$

Heisenberg uncertainty
results in larger
displacements for H than D.

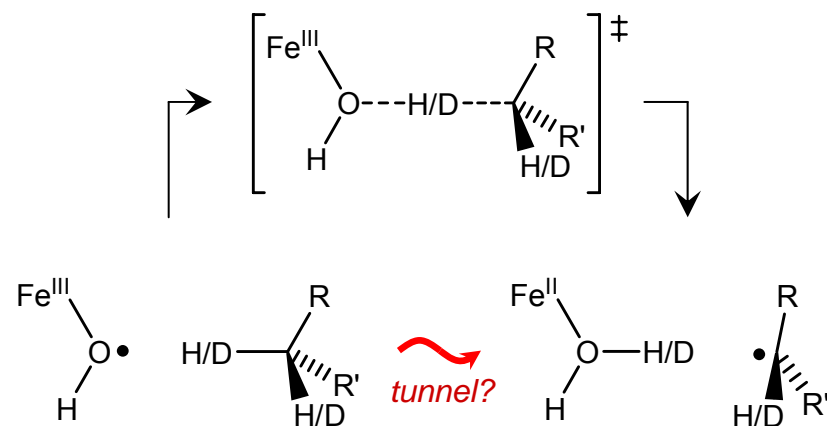
*So, H "tunnels" through
barriers better than D.*



Isotope Effects and Tunneling



Crystal structure, soybean lipoxygenase w/ linoleic acid



Hypothesis:

Enzyme operates by forcing H(D) into tunneling distance ($< \lambda$).

Isotope Effects and Tunneling

Important feature of tunneling:

de Broglie wavelength λ much less sensitive to temperature than rate constants k .

So, if

$$k_{\text{obs}} = k_{\text{thermal}} + k_{\text{tunneling}},$$

